



$\hat{v} = \frac{\vec{v}}{|\vec{v}|}$ is the unit vector along \vec{v}

(a) Straight line:

$$\vec{r} = \vec{r}_0 + \lambda \hat{v} = \vec{r}_0 + \lambda \frac{\vec{v}}{|\vec{v}|}$$

(b) $d = |\vec{r}_0 - \vec{r}| \sin \theta = |(\vec{r}_0 - \vec{r}) \times \hat{v}|$

$$d = \frac{|(\vec{r}_0 - \vec{r}) \times \hat{v}|}{|\hat{v}|}$$

When the tip of \vec{r} is on the line, $\vec{r}_0 - \vec{r}$ is parallel to \hat{v} , so the cross product vanishes and $d=0$, as it should.

(c) $\vec{w} = \frac{(\vec{r}_0 - \vec{r}) \cdot \hat{v}}{|\hat{v}|} \hat{v} = \underbrace{(\vec{r}_0 - \vec{r}) \cdot \hat{v}}_{\text{projection of } \vec{r}_0 - \vec{r} \text{ onto } \hat{v}} \hat{v}$

$$\vec{w} = \frac{(\vec{r}_0 - \vec{r}) \cdot \hat{v}}{|\hat{v}|} \hat{v} = \vec{r}_0 - \vec{r} + \underbrace{\left[\frac{(\vec{r}_0 - \vec{r}) \cdot \hat{v}}{|\hat{v}|} - 1 \right] \hat{v}}_0$$

When the tip of \vec{r} is on the line, $\vec{w} = \vec{r}_0 - \vec{r}$, as it should.